

**O K L A H O M A   S T A T E   U N I V E R S I T Y**  
**S C H O O L   O F   E L E C T R I C A L   A N D   C O M P U T E R   E N G I N E E R I N G**



**ECEN 3413 Controls I**  
**Spring 1998**  
**Final Exam**



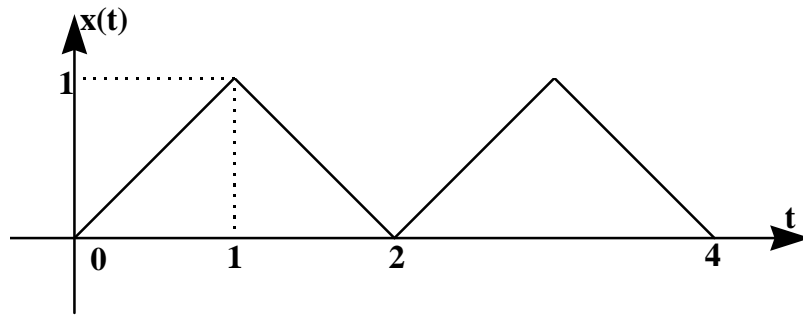
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**Problem 1:** (*Laplace transform*)

Determine the Laplace transform of the following signal,  $x(t)$ , with six periods (only two periods are shown in the graph).



**Problem 2:** (*z transform*)

A discrete-time system has the transfer function

$$H(z) = \frac{-0.4z^{-1} - 0.5z^{-2}}{1 - 1.3z^{-1} + 0.4z^{-2}},$$

- a) find an analytical expression for the step response.
- b) write a MATLAB program to find the impulse response (as accurate as you could).

**Problem 3:** (*time response*)

Determine the transfer function  $E_o(s)/E_i(s)$  of the electrical circuit shown below. Suppose that the input  $e_i(t)$  is given by

$$e_i(t) = \begin{cases} E_i & 0 < t < t_1 \\ 0 & \text{elsewhere} \end{cases}.$$

Obtain the output  $e_o(t)$ . Assume that  $R_2 = 1.5R_1$ ,  $C_2 = C_1$ , and  $R_1C_1 = 1$ . Assume also that the initial charges in the capacitors are zero.

**Problem 4:** (*frequency response*)

Consider the electrical circuit shown below. If the input voltage  $e_i(t) = E_i \cos \omega t$ , what is the output voltage  $e_o(t)$  at steady state ?